# The Conformational Analysis of Saturated Heterocycles. Part L. ${ }^{1}$ Computer Program for Strain Energy Minimisation in Six-membered Rings and Recalculation of Conformational Equilibria 

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#### Abstract

Computer programs are developed which allow (a) the calculation of ring geometry including vector angles for dipole-moment components and ( $b$ ) the energy minimisation of bond and torsion angle strain. Conformational equilibria are recalculated for 1 -alkylpiperidines, 1,3-dialkylhexahydropyrimidines, 3 -alkyltetra-hydro-1,3-oxazines, 5 -alkyldihydro-1,3,5-dithiazines, and 1,3,5-trialkylhexahydro-1,3,5-triazines. The previous conclusions are little, for the most part insignificantly, affected.


As our studies ${ }^{2-8}$ of the conformations of saturated sixmembered rings have progressed to less-symmetrical rings containing several heteroatoms, geometrical difficulties in the interpretation of dipole moments have increased. Two types of problems were encountered: (i) the plain calculation of angles between component dipole vectors in unsymmetrical rings and (ii) the question of allowance for torsional strain, and the minimisation of total bond-angle and torsional strain. The present paper describes our proposed solution of this problem, and consequent recalculations for the conformational equilibria previously reported. The approach used has been based on a well-developed classical mechanical model ${ }^{9}$ but extends the range of molecules studied into experimentally untested polyheterocyclic systems.

Strain Energy Minimisation.-A ring consisting of $n$ atoms is characterised by $3 n-6$ independent parameters. For a six-membered ring existing in the chair form, the 12 independent parameters may be chosen from the $3 n$ internal co-ordinates: 6 bond lengths, 6 bond angles, and 6 torsional angles. We have chosen the 6 bond angles and 6 bond lengths as the independent parameters, and have devised a program to express the 18 Cartesian co-ordinates of the ring atoms in these terms. ${ }^{10}$

The total strain energy of a given conformation, equation (1), is the sum of several components: $E_{\theta}$ is the

$$
\begin{equation*}
E_{\text {total }}=E_{\theta}+E_{\omega}+E_{\mathrm{R}}-E_{\mathrm{A}}+E_{1} \tag{1}
\end{equation*}
$$

angle strain, $E_{\omega}$ the torsional strain, $E_{\mathrm{R}}$ and $E_{\mathrm{A}}$ the repulsive and attractive non-bonded interactions, and $E_{l}$ the bond-length distortion strain. The strain energy
1 Part XLIX, M. J. Cook, R. A. Y. Jones, A. R. Katritzky, M. Moreno-Mañas, A. C. Richards, A. J. Sparrow, and D. L. Trepanier, preceding paper.
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${ }^{3}$ R. A. Y. Jones, A. R. Katritzky, and M. Snarey, J. Chem. Soc. $(B), 1970,131$.

4 R. A. Y. Jones, A. R. Katritzky, and M. Snarey, J. Chem. Soc. (B), 1970, 135.

5 R. A. Y. Jones, A. R. Katritzky, and D. L. Trepanier, J. Chem. Soc. (B), 1971, 1300.
${ }_{6}$ R. A. Y. Jones, A. R. Katritzky, D. L. Ostercamp, K. A. F. Record, and A. C. Richards, J.C.S. Perkin II, 1972, 34.
for a structure with known geometry is calculated by applying the appropriate potential functions, and forming the sum of their various contributions. This approximate structure is then altered so as to minimise the energy, using the method of conjugate gradients. ${ }^{11,12}$ As we assume invariant bond lengths (see later), this requires the minimisation of a function of up to six variables.

As a second approach we have used the method of steepest descent to find the strain-energy minimum. ${ }^{9}$ In this method, the derivatives are estimated by changing each angle in turn by a given amount, and recalculating the energy for each of these six modified conformations, thus requiring the evaluation of the energies of seven conformations including the original. Each of the original bond angles is next changed by an amount proportional to the partial derivative and a new energy is calculated. The angles are modified in this way until the total energy no longer decreases. A new set of partial derivatives is then calculated and the angles of the ring are then changed in this sense. These processes are then continued until an energy minimum is reached. We recognise this as a local, and not a global energy minimum.

If the structure contains symmetry elements, the symmetrically related atoms are changed simultaneously in calculating the steepest descent partial derivatives. In the conjugate gradient method certain symmetry elements can be kept, and this decreases computational time.

The two methods used do not require the formal evaluation of derivatives, and may locate false minima. They do, however, locate nearly identical minima, which suggests that they represent approximations to

[^0]the true minimum. The convergence of the conjugate gradient method is more rapid, and the following discussion is in terms of the results obtained by this method.

Potential Functions.-(a) Bond-length distortion. The change in energy with bond-length distortion for small displacements may be evaluated from equation (2),

$$
\begin{equation*}
\Delta V=\frac{1}{2} k_{r}\left(r-r_{0}\right)^{2} \tag{2}
\end{equation*}
$$

where $r_{0}$ is the equilibrium bond length, and $k_{r}$ is the stretching-force constant. The force constant $k_{r}$ for a $\mathrm{C}-\mathrm{C}$ bond is near $5 \times 10^{5}$ dyn $\mathrm{cm}^{-1}$ from vibrational spectral data. ${ }^{13}$ However, following Hendrickson ${ }^{14}$ we neglect this contribution and treat bond lengths as invariant, because the energy required to change them appreciably is much greater than the energy required to change valence angles or torsional angles. The bond lengths used ${ }^{15}$ are: $\mathrm{C}-\mathrm{C} 1.54, \mathrm{C}-\mathrm{N} 1 \cdot 47, \mathrm{C}-\mathrm{O} 1 \cdot 43$, and C-S $1.81 \AA$.
(b) Bond-angle distortion. The energy associated with the bending of a single bond angle from its strain-free value is given by equation (3) where $k_{\theta}$ is the bending

$$
\begin{align*}
E_{\theta} & =\frac{1}{2} k_{\theta}\left(\theta-\theta_{0}\right)^{2}  \tag{3}\\
V & =\frac{1}{2} \Sigma k_{\theta}\left(\Delta \theta_{\mathrm{i}}\right)^{2} \tag{4}
\end{align*}
$$

force constant and $\theta_{0}$ is the strain-free bond angle. ${ }^{14}$ Hence the total bond-angle strain is given by equation (4).

Hendrickson ${ }^{14}$ used Westheimer's ${ }^{16}$ force constants, which are $0.32,0.55$, and $0.8 \mathrm{mdyn} \AA \mathrm{rad}^{-2}$ for the $\mathrm{H}-\mathrm{C}-\mathrm{H}, \mathrm{C}-\mathrm{C}-\mathrm{H}$, and $\mathrm{C}-\mathrm{C}-\mathrm{C}$ respectively, and combined these to obtain a single equivalent force constant of 0.9 mdyn $\AA \mathrm{rad}^{-2}$ for $\mathrm{C}-\mathrm{CH}_{2}-\mathrm{C}$ bending (cf. ref. 9 ). Other values for the bending force constants for $\mathrm{C}-\mathrm{C}-\mathrm{C}$ are 0.97 (ref. 17) and 0.86 (ref. 18) mdyn $\AA \operatorname{rad}^{-2}$ from normal mode analysis of cyclohexane, and $0.90 \mathrm{mdyn} \AA$ $\mathrm{rad}^{-2}$ from normal mode analysis of $n$-alkanes. ${ }^{19}$ The calculated potential is not very sensitive to the value of the force constant used. ${ }^{20}$ For $\mathrm{C}-\mathrm{C}-\mathrm{C}$ we used 0.9 mdyn $\AA \operatorname{rad}^{-2}$ (ref. 19).

Less work relevant to the calculation of force constants has been done on molecules incorporating heteroatoms. No literature information is directly relevant to the nitrogen systems, though Hendra and Powell ${ }^{21}$ suggested from a comparison of values for amines and alcohols that the bending force constants for $\mathrm{C}-\mathrm{C}-\mathrm{N}$ and $\mathrm{C}-\mathrm{N}-\mathrm{C}$ should be 0.9 and 1.38 mdyn $\AA \mathrm{rad}^{-2}$, respectively. Normal mode analysis of aliphatic ethers ${ }^{22}$ and of a number of oxans ${ }^{18}$ has indicated respectively 1.18 and 1.15 mdyn $\AA \mathrm{rad}^{-2}$ for $\mathrm{C}-\mathrm{C}-\mathrm{O}$ and 1.31 and $1.02 \mathrm{mdyn} \AA$ $\mathrm{rad}^{-2}$ for $\mathrm{C}-\mathrm{O}-\mathrm{C}$. In similar fashion the $\mathrm{C}-\mathrm{S}-\mathrm{C}$ force constant has been reported variously ${ }^{23}$ as 1.02 and

[^1]1.42 mdyn $\AA \mathrm{rad}^{-2}$. For $\mathrm{X}-\mathrm{C}-\mathrm{Y}$ systems no data was available. Since, over a small range, the calculated geometries were insensitive to the actual values of the force constants used, selection of values was made by interpolation of the available data. These are collected in Table 1.

Table 1
Angle force constants ( $k_{\theta}, \operatorname{mdyn} \AA \operatorname{rad}^{-2}$ )

| X | $\mathrm{C}-\mathrm{C}-\mathrm{X}$ | $\mathrm{C}-\mathrm{X}-\mathrm{C}$ | $\mathrm{X}-\mathrm{C}-\mathrm{X}$ | $\mathrm{X}-\mathrm{C}-\mathrm{Y}$ |
| :---: | :---: | :---: | :---: | :---: |
| C | $\begin{gathered} 0.9 \\ \left(0.9, a 0 \cdot 97,{ }^{b}\right. \\ 0.86, c 0 \cdot 90^{d} \end{gathered}$ | $0 \cdot 9$ | 0.9 |  |
| N | $\begin{gathered} 1 \cdot 0 \\ \left(0 \cdot 9^{e}\right) \end{gathered}$ | $\begin{gathered} 1.0 \\ \left(1.38^{e}\right) \end{gathered}$ | 1.2 | $(\mathrm{Y} \stackrel{1 \cdot 3}{=} \mathrm{S})$ |
| 0 | $\stackrel{1 \cdot 2}{\left(1 \cdot 18,{ }^{d} 1 \cdot 15^{c}\right)}$ | $\begin{gathered} 1 \cdot 1 \\ \left(1.02,{ }^{c} 1 \cdot 311^{d}\right) \end{gathered}$ | $\begin{gathered} 1.6 \\ \left(1.66^{c}\right) \end{gathered}$ | $(\mathrm{Y} \stackrel{1.4}{=} \mathrm{N})$ |
| S | $1 \cdot 1$ | $\stackrel{1 \cdot 2}{\left(1 \cdot 02,{ }^{f} 1 \cdot 42^{g}\right)}$ | 1.4 | $(\stackrel{1.5}{=} \mathrm{O})$ |

${ }^{a}$ Ref. 14. ${ }^{b}$ Ref. 17. ${ }^{c}$ Ref. 18. ${ }^{a}$ Ref. 22. © Ref. 21. Ref. 23a. ${ }^{s}$ Ref. $23 b$.
(c) Equilibrium bond angles. The bond angles used (Table 2) are taken from corresponding three-membered units, e.g. $\mathrm{C}-\mathrm{O}^{-} \mathrm{C} 111 \cdot 5^{\circ}$ from dimethyl ether, as listed by Sutton. ${ }^{15}$

Table 2
Equilibrium bond angles

| Angle | Equilibrium <br> bond angle <br> $\left(\theta_{0}{ }^{\circ}\right)$ |
| :--- | :---: |
| CCC | $112 \cdot 4^{a}$ |
| CCN | $110 \cdot 0^{a}$ |
| CCO | $110 \cdot 0^{a}$ |
| CCS | $113 \cdot 0^{a}$ |
| CNC | $112 \cdot 1^{d}$ |
| COC | $111 \cdot 5^{a}$ |
| CSC | $99 \cdot 0^{c}$ |
| NCN | $110 \cdot 0^{d}$ |
| OCO | $110 \cdot 0^{d}$ |
| SCS | $110^{d}$ |
| NCO | $110 \cdot 0^{d}$ |
| NCS | $110 \cdot 0^{d}$ |

a ' Interatomic Distances,' ed. L. E. Sutton, Chemical Society Special Publication, No. 11, London, 1958, p. M139.
${ }^{b}$ N. L. Allinger, J. A. Hirsch, and M. A. Miller, Tetrahedron Letters, 1967, 3729. © L. Pierce and M. Hayashi, J. Chem. Phys., 1961, 35, 479. a Assumed value.
(d) Torsional distortion. As Bixon and Lifson pointed out, ${ }^{20}$ this mode of distortion expends the least amount of energy in a cyclic structure and consequently large torsional angle changes may be found.

Bixon and Lifson pointed out that, on the basis of the enthalpy difference between gauche isomers of the higher n-alkanes, ${ }^{24}$ an unsymmetrical barrier might be expected. The potential barriers for rotation in cyclohexane are considered ${ }^{25}$ to be quite high. It is certain

[^2]that the torsional barrier is indeed unsymmetrical, but it is not clear in which sense this will be (whether distortion to $\omega>60^{\circ}$ will in fact be more difficult than distortion to $\omega<60^{\circ}$ (where $\omega$ is the dihedral angle between the two ring bonds). Since the uncertainties in the degree of asymmetry are large, and for the sake of simplicity, a symmetrical threefold sinusoidal barrier has been used, following Bixon and Lifson 20 and others. ${ }^{9,26,27}$ This is described by equation (5), where
\[

$$
\begin{equation*}
E_{\omega}=\frac{1}{2} k_{t}(1+\cos 3 \omega) \mathrm{kcal} \mathrm{~mol}^{-1} \tag{5}
\end{equation*}
$$

\]

the torsional distortional energy $\left(E_{\omega}\right)$ is defined by the sinusoidal function and by the observed barrier height in the 'three heavy atom' system ( $K_{t} \mathrm{kcal} \mathrm{mol}{ }^{-1}$ ). The 'three heavy atom' systems were chosen because, as Bixon and Lifson found, ${ }^{20}$ the propane barrier gives good agreement between the strain energy minimised angles and the observed values for cyclohexane. ${ }^{28}$ The values of barriers to rotation ${ }^{29}$ for the three-atom systems used in our calculations are given in Table 3.

Table 3
Barriers to rotation of three-membered units ${ }^{29}$
Segment
C-C-C
$\mathrm{C}-\mathrm{O}-\mathrm{C}$
$\mathrm{C}-\mathrm{N}-\mathrm{C}$
$\mathrm{C}-\mathrm{S}-\mathrm{C}$
Barrier $\left(K_{\mathbf{T}}\right)$
(kcal mol ${ }^{-1}$ )
$3 \cdot 4$
$2 \cdot 7$
$3 \cdot 6$
$2 \cdot 1$
(e) Non-bonded interactions. It is difficult to assess accurately the contribution to the total strain energy

Table 4
Bond and torsional angles and Cartesian co-ordinates


Piperidine

(2)
$\begin{array}{rr} & \\ 1 & 0.0000 \\ 2 & -1.0595 \\ 3 & -1.3014 \\ 4 & 0.0000 \\ 5 & 1.1076 \\ 6 & 1.2793\end{array}$

| 0.0000 | 0.0000 |
| ---: | ---: |
| 0.7240 | -0.7170 |
| 2.0916 | -0.0595 |
| 2.9128 | 0.0000 |
| 2.0917 | 0.6860 |
| 0.7240 | 0.0000 |

Piperazine

|  | 1 | $0 \cdot 0000$ | $0 \cdot 0000$ | $0 \cdot 0000$ |
| :---: | :---: | :---: | :---: | :---: |
| $57.4{ }^{\circ}$ | 2 | -1.0639 | $0 \cdot 7429$ | -0.6908 |
| $\pm 0.3$ | 3 | -1.2685 | $2 \cdot 1066$ | $0 \cdot 0058$ |
|  | 4 | $0 \cdot 0000$ | $2 \cdot 8494$ | $0 \cdot 0000$ |
| ${ }_{ \pm 0.9}^{58.7}$ | 5 | 1.0670 | $2 \cdot 1066$ | $0 \cdot 6859$ |
|  | 6 | $1 \cdot 2685$ | $0 \cdot 7429$ | $0 \cdot 0000$ |

(3)
Hexahydropyrimidine


|  |  |  |  |
| :--- | ---: | ---: | ---: |
| 1 | 0.0000 | 0.0000 | 0.0000 |
| 2 | -1.0548 | 0.7614 | -0.6845 |
| 3 | -1.3111 | 2.0556 | -0.0250 |
| 4 | 0.0000 | 2.8630 | 0.0000 |
| 5 | 1.1197 | 2.0556 | 0.6826 |
| 6 | 1.2575 | 0.7614 | 0.0000 |

Tetrahydro-1,3-oxazine


| 1 | 0.0000 | 0.0000 | 0.0000 |
| ---: | ---: | ---: | ---: |
| 2 | -1.0534 | 0.7465 | -0.7029 |
| 3 | -1.3222 | 2.0440 | -0.0552 |
| 4 | 0.0000 | 2.8316 | 0.0000 |
| 5 | 1.0934 | 1.9887 | 0.6824 |
| 6 | 1.2241 | 0.7393 | 0.0000 |

(5)

Table 4 (Continued)
Cartesian co-ordinates of atoms
$\begin{array}{lll}\mathrm{X} & \stackrel{(\AA)}{\mathrm{Y}}{ }^{\mathrm{c}} & \mathrm{Z}\end{array}$

Tetrahydro-1,4-dioxan

(6)

Hexahydro-1,3,5-triazine

(7)

1,3,5-Trioxan


|  |  |  |  |
| ---: | ---: | ---: | ---: |
| 1 | 0.0000 | 0.0000 | 0.0000 |
| 2 | -1.0367 | 0.7378 | -0.6525 |
| 3 | -1.2187 | 1.9997 | 0.0058 |
| 4 | 0.0000 | 2.7479 | 0.0000 |
| 5 | 1.0344 | 1.9997 | 0.6443 |
| 6 | 1.2250 | 0.7378 | 0.0000 |

(8)

Dihydro-1,3,5-dithiazine


| 1 | 0.0000 |
| ---: | ---: |
| 2 | -1.0495 |
| 3 | -1.5691 |
| 4 | 0.0000 |
| 5 | 1.2397 |
| 6 | 1.2991 |


| 0.0000 | 0.0000 |
| :--- | ---: |
| 0.6880 | -0.7656 |
| 2.2192 | 0.0415 |
| 3.1205 | 0.0000 |
| 2.2192 | 0.9628 |
| 0.6880 | 0.0000 |

(9)
${ }^{a}$ Convergence to $0.05^{\circ}$ variation in bond angles (at apices). Dihedral (torsional) angles are given midway along relevant bonds. ${ }^{6}$ Co-ordinates for tetrahydro-1,3-dioxan and tetra-hydro-1,3-dithian were also calculated.
from non-bonded interactions especially in heterocyclic systems. To some extent they are already allowed for 26 H. M. Seip, Acta Chem. Scand., 1969, 23, 2741.
27 N. C. Cohen, Tetrahedron, 1971, 27, 789.
${ }^{28}$ H. R. Buys and H. J. Geise, Tetrahedron Letters, 1970, 2991.
29 J. P. Lowe, Progr. Phys. Org. Chem., 1968, 6, 1.
in that the force constants for angle bending and torsional twisting, derived from spectroscopic measurements, undoubtedly contain contributions from nonbonded interactions. Thus Allinger et al., ${ }^{30}$ who have specifically included terms for non-bonded interactions in their strain-energy calculations, use abnormally low values for bending and torsional force constants. Since we cannot readily assess the extent of the redundancy nor can we easily parameterise the total non-bonded interactions we have chosen to omit a separate term for them; Seip ${ }^{26}$ found that this term made little difference to the five-membered ring molecules that he was studying.

## RESULTS

The bond and torsional angles and Cartesian coordinates given in Table 4 were calculated with the












Angles between ring planes, calculated from atom co-ordinates of Table 4. * For hexahydro-1,3,5-triazine, angle between equatorial lone pairs $=106 \cdot 9^{\circ}$, between axial lone pairs $=1.6^{\circ}$, angle between axial and equatorial lone pairs $=112.0^{\circ}$

ICL 1905E computer at the University of East Anglia using the potential functions and parameters given above. The results obtained from the conjugate gradient program GEOMIN are given. ${ }^{10}$ The angles between planes, calculated from the atom co-ordinates, are given in the Figure.
${ }^{30}$ N. L. Allinger, J. A. Hirsch, M. A. Miller, I. J. Tyminski, and E. A. van Catledge, J. Amer. Chem. Soc., 1968, 90, 1199.
${ }_{31}$ M. Davis and O. Hassel, Acta Chem. Scand., 1963, 17, 1181.
${ }^{32}$ A. Yokozeki and K. Kuchitsu, Bull. Chem. Soc. Japan, 1971, 44, 2352.
${ }^{33}$ A. H. Clark and T. G. Hewitt, J. Mol. Structure, 1971, 9, 33. ${ }^{34}$ R. A. Y. Jones, A. R. Katritzky, A. C. Richards, and R. J. Wyatt, J. Chem. Soc. (B), 1970, 122.

## DISCUSSION

For cyclohexane, for which electron-diffraction data have been reported, the calculated values of bond and torsional angles are very close to the experimentally observed ones (Table 5). Considering the variation

Table 5
Comparison of experimental and calculated parameters for six-membered rings

| Calculated |  | Experimental |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Bond angle ( ${ }^{\circ}$ ) | Torsional angle ( ${ }^{\circ}$ ) | Bond angle ( ${ }^{\circ}$ ) | Torsional angle ( ${ }^{\circ}$ ) | Ref. |
| Cyclohexane |  |  |  |  |
| CCC 111•1 | $55 \cdot 9$ | $111.05 \pm 0.15$ | $55 \cdot 9 \pm 0 \cdot 3$ | $a$ |
| Piperazine |  |  |  |  |
| CNC 111.7 | $58.7 \pm 0 \cdot 1$ | $112.6 \pm 0.5$ |  | $b$ |
|  |  | $109.0 \pm 0 \cdot 8$ |  | $c$ |
| CCN 109.4 $\pm 0 \cdot 1$ | $57 \cdot 4 \pm 0 \cdot 3$ | $109.8 \pm 0.5$ |  | $b$ |
|  |  | $110.4 \pm 0.8$ |  | $c$ |
| 1,4-Dioxan |  |  |  |  |
| COC 111.2 | $58 \cdot 8 \pm 0 \cdot 2$ | $112.5 \pm 0.5$ |  | $b$ |
| CCO 109.6 $\pm 0.2$ | $57 \cdot 8 \pm 0 \cdot 3$ | $109.2 \pm 0.5$ |  | $b$ |
| 1,3,5-Trioxan |  |  |  |  |
| COC 110.7 $\pm 0.1$ | $58 \cdot 0 \pm 0.3$ | $110 \pm 1 \cdot 0$ |  | $d$ |
|  |  | $109.2 \pm 1 \cdot 0$ |  | $e$ |
| OCO 109.9 $\pm 0 \cdot 2$ | $58.0 \pm 0.3$ | $110 \pm 2 \cdot 0$ |  | $d$ |
|  |  | $111.0 \pm 0.7$ |  | $c$ |

${ }^{a}$ Ref. 28. ${ }^{b}$ Ref. 31. ${ }^{c}$ Ref. 32. ${ }^{a}$ S. Kimura and K. Aoki, J. Chem. Soc. Japan, Pure Chem. Sect., 1951, 72, 169. • Ref. 33.
reported in electron-diffraction data for piperazine ${ }^{31,32}$ and 1,3,5-trioxan, ${ }^{31,33}$ the angles calculated for these and for 1,4 -dioxan are also in good agreement with the experimentally observed values. The calculations on other molecules have used the same parameters, or parameters from similar sources, and therefore should give reasonable representations of the molecules studied.

The results suggest that substitution of carbon in the cyclohexane ring by nitrogen or oxygen leads to some puckering at the substituted end of the ring. The effect of the small sulphur valency angle and the long $\mathrm{C}-\mathrm{S}$ bond is to pucker the ring severely at the $\mathrm{S}-\mathrm{C}-\mathrm{S}$ plane in 1,3-dithian (Figure).

The previously reported dipole moment results for the $N$-alkyl axial-equatorial equilibria in 1-alkyl-4-arylpiperidines, ${ }^{34} 1,3$-dialkylhexahydropyrimidines, ${ }^{3} 3$-alkyl-tetrahydro-1,3-oxazines, ${ }^{5}$ 1,3,5-trialkylhexahydro-1,3,5triazines, ${ }^{4} 5$-alkyldihydro-1,3,5-dithiazines, ${ }^{35}$ and 1-alkyl-4-t-butylpiperazines ${ }^{36}$ have been calculated, making the same assumptions used in the original work, except that the strain-energy minimised geometry has been used. The original and recalculated results are summarised in Table 6.

For the 1-alkyl-4-t-butylpiperazines, the diaxial and diequatorial conformers are almost centrosymmetric and probably possess very small dipole moments arising

[^3]from the different $\mathrm{C}-\mathrm{N}-\mathrm{C}$ bond angles caused by the $N$-alkyl and $N$-t-butyl substituents; the axial-equatorial conformers possess dipole moments the components of which are dependent on their angles to the $\mathrm{C}-\mathrm{N}-\mathrm{C}$ plane. This situation shows the limitation of the programs used: the effect of exocyclic substituents on the bond angles in the ring cannot easily be expressed without explicit consideration of non-bonded interactions and for the same reason the angle between the
ethyl, and isopropyl respectively. The conformational free-energy of an axial t-butyl group in 1,3,5-tri-t-butyl-hexahydro- $1,3,5$-triazine is found to be somewhat lower $\left(0 \cdot 20 \mathrm{kcal} \mathrm{mol}^{-1}\right)$ than previously estimated $(0.35 \mathrm{kcal}$ $\left.\mathrm{mol}^{-1}\right) .{ }^{4}$
The results for the 1,3 -dialkylhexahydropyrimidines, 3 -alkyltetrahydro-1,3-oxazines, and 5 -alkyldihydro-$1,3,5$-dithiazines are very nearly unchanged. This suggests that the original estimates of the ring geometry

Table 6
Recalculated results for some conformational equilibria ${ }^{a}$

|  | Optimised geometry |  | Previous results |  |
| :---: | :---: | :---: | :---: | :---: |
| Alkyl group(s) <br> 1-Alkylpiperidines ${ }^{\boldsymbol{b}}$ | \% Alkyl equatorial | $\Delta G^{\circ}{ }_{25}$ <br> (kcal mol ${ }^{-1}$ ) | \% Alkyl equatorial | $\Delta G^{\circ}{ }_{25}$ <br> (kcal mol${ }^{-1}$ ) |
| 1-Alkylpiperidines | equatorial 75 | (kcal mol 0.65 | equatorial 73 | $\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ 0.59 |
| Ethyl | 85 | 1.03 | 83 | 0.95 |
| Isopropyl | 94 | 1.58 | 92 | $1 \cdot 44$ |
| 1,3-Dialkylhexahydropyrimidines ${ }^{\text {c }}$ | \% Alkyl groups diequatorial | $\begin{gathered} \Delta G^{\circ}{ }_{25}{ }^{d} \\ \text { for 3-alkyl } \\ \left(\mathrm{kcal} \mathrm{~mol}^{-1}\right) \end{gathered}$ | \% Alkyl groups diequatorial | $\begin{gathered} \Delta G^{\circ}{ }_{25}^{d} \\ \text { for 3-alkyl } \\ \left(\text { kcal } \mathrm{mol}^{-1}\right) \end{gathered}$ |
| Dimethyl | 54 | 0.51 | 55 | $0 \cdot 54$ |
| Diethyl | 57 | $0 \cdot 59$ | 59 | $0 \cdot 62$ |
| Di-isopropyl | ca. 100 | $\geqslant 2.0$ | ca. 100 | $\geqslant 1.8$ |
| Di-t-butyl | 100 | - | 100 | - |
| 1-t-Butyl-3-methyl | 68 | $0 \cdot 43$ | 69 | $0 \cdot 47$ |
| 1-t-Butyl-3-ethyl | 75 | $0 \cdot 64$ | 75 | $0 \cdot 65$ |
| 1-t-Butyl-3-isopropyl | 100 | - | ca. 100 | $\geqslant 1.5$ |
| 3-Alkyltetrahydro-1,3-oxazines ${ }^{\text {e }}$ | \% Alkyl equatorial | $\begin{gathered} \Delta G_{25}^{\circ} \\ \text { (kcal mol }{ }^{-1} \text { ) } \end{gathered}$ | \% Alkyl equatorial | $\begin{gathered} \Delta G_{25}^{\circ} \\ (\mathrm{kcal} \mathrm{~mol} \\ \end{gathered}$ |
| Methyl | 57 | $0 \cdot 18$ | 58 | $0 \cdot 20$ |
| Eth;l | 66 | $0 \cdot 40$ | 68 | $0 \cdot 43$ |
| Isopropyl |  |  | 86 | 1.06 |
| t-Butyl | 100 | - | ca. 100 | -- |
| 1,3,5-Trialkylhexahydro-1,3,5-triazines ${ }^{\text {f }}$ | \% Mono-axial alkyl | $\begin{gathered} \Delta G_{25}^{\circ} \\ \left(\mathrm{kcal} \mathrm{~mol}^{-1}\right) \end{gathered}$ | \% Monoaxial alkyl | $\left.\begin{array}{c} \Delta G^{\circ}{ }_{25}{ }^{g} \\ (\mathrm{kcal} \mathrm{~mol} \end{array}\right)$ |
| Isopropyl | 91 | $0 \cdot 72$ | 92 | $0.80 \pm 0.20$ |
| t-Butyl | 81 | $0 \cdot 20$ | 85 | $0.35 \pm 0.12$ |
| 5-Alkyldihydro-1,3,5-dithiazines ${ }^{\boldsymbol{h}}$ | $\begin{aligned} & \text { \% Alkyl } \\ & \text { axial } \end{aligned}$ | $\begin{gathered} \Delta G_{25}^{\circ} \\ (\text { kcal mol } \end{gathered}$ | \% Alkyl axial | $\begin{gathered} \Delta G^{\circ}{ }_{25} \\ \text { (kcal mol} \left.{ }^{-1}\right) \end{gathered}$ |
| Methyl, ethyl, isopropyl t-Butyl | 100 81 | $\overline{0.84}$ | $\begin{aligned} & 100 \\ & 82-75 \end{aligned}$ | 0.65-0.90 ${ }^{\text {i }}$ |

${ }^{a}$ In cyclohexane at $25^{\circ}$. ${ }^{b}$ Using data for the 1 -alkyl- and 1 -alkyl-4-p-chlorophenyl-piperidines (ref. 34). © See ref. 3. ${ }^{d}$ Corrected in the dimethyl, diethyl and di-isopropyl compounds for two-fold degeneracy of the equatorial, axial conformers. ${ }^{3}$ - In benzene at $25^{\circ}$ (ref. 5). ${ }^{f}$ Considering the symmetrical trialkyl compounds where the equilibrium effectively contains only the triequatorial and mono-axial, diequatorial conformers (ref. 4). ${ }^{g}$ Corrected for three-fold axis of symmetry in the triequatorial alkyl conformer (ref. 4). ${ }^{h}$ Ref. $35 .^{\text {i }}$ See ref. 35 for a discussion of this range of values.
$\mathrm{C}-\mathrm{N}-\mathrm{C}$ plane and the resultant moment has to be taken from another source. ${ }^{37}$

The recalculated results show a small increase in the estimated values of $\Delta G^{\circ}{ }_{25}$ for $N$-alkyl groups in piperidine by $0.06-0.15 \mathrm{kcal} \mathrm{mol}^{-1}$ above the values previously reported; ${ }^{34}$ the largest increase is for the N -isopropyl compound. The values remain less than those for $C$-alkyl groups in cyclohexane, where the preferred values ${ }^{38}$ are $1 \cdot 7,1 \cdot 8$, and $2 \cdot 1 \mathrm{kcal} \mathrm{mol}^{-1}$ for methyl,
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were not greatly in error, and also reflects the fact that in the systems chosen the calculated results were not too sensitive to the molecular geometry. We conclude that dipole-moment-derived conclusions regarding the conformations of heterocycles can be confidently accepted, and that a simple physical model satisfactorily describes the geometry of the cyclohexane ring and related heterocycles.
[2/1347 Received, 12th June, 1972]

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